Name:

Show that the series

$$\sum_{n=1}^{\infty} \frac{\sin(nx)}{n^2}$$

converges for each $x \in \mathbb{R}$, and denote the sum by $f(x)$. Is f continuous on $[0, \pi]$? Can you compute $\int_0^\pi f(x)\, dx$?